

Glazer & Mark.

7.5. At 1keV, density of 10^{33} m^{-3} , is electron Fermi-Dirac or Maxwell-Boltzmann?

$$\rho = 10^{33} \text{ m}^{-3}, \quad m = 0.5 \times 10^6 \text{ eV}/c^2,$$
$$k_B T = 10^3 \text{ eV},$$
$$h = 4.14 \times 10^{-15} \text{ eV s}$$

$$\Rightarrow \frac{V}{N} \left(\frac{2\pi m k_B T}{h^2} \right)^{3/2}$$

$$\approx \frac{1}{\rho} \left(\frac{6 \times 0.5 \times 10^6 \text{ eV} \times 10^3 \text{ eV} \times \text{s}^2}{c^2 \text{ m}^2 \times (4.14 \times 10^{-15})^2 \text{ eV}^2 \text{ s}^2} \right)^{3/2}$$

$$= \frac{\text{m}^3}{10^{33}} \left(\frac{3 \times 10^6 \times 10^3 \times \cancel{\text{eV}} \times \cancel{\text{s}^2}}{(3 \times 10^8)^2 \times (4.14 \times 10^{-15})^2 \times \cancel{\text{eV}}^2 \times \cancel{\text{s}^2} \times \text{m}^2} \right)^{3/2}$$

$$\approx \frac{\text{m}^3}{10^{33}} \left(\frac{3 \times 10^9}{10^{17} \times 10^{-29} \text{ m}^2} \right)^{3/2}$$

$$\approx \frac{\text{m}^3}{10^{33}} \left(3 \times 10^{21} \right)^{3/2} \approx 10^{-1.5}$$

since $10^{-1.5}$ is not greatly larger than 1,
we can not use Maxwell-Boltzmann Dist.